Acid Base Equilibria

Bronsted-Lowry Definition of acid Base behaviour



Calculating pH of a Strong Base



Calculating pH of a Weak Acid

To make the calculation easier two assumptions are made to simplify the Ka expression:	Ka=	[<u>H⁺ _(aq)][A⁻ _(aq)]</u>
 [H⁺ (aq)]_{eqm} = [A⁻ (aq)] eqm because they have dissociated according to a 1:1 ratio. 	Simplif	ies to \downarrow
 As the amount of dissociation is small we assume that the initial concentration of the undissociated acid has remained constant. 	Ka=	[H ⁺ _(aq)] ²
So [HA $_{(aq)}$] $_{eqm} = [HA_{(aq)}]$ initial		Luco (aq)Jinitial

Example 5 What is the pH of a solution of 0.01 mol dm⁻³ ethanoic acid (ka is 1.7 x 10⁻⁵ mol dm⁻³)? $CH_3CO_2H_{(aq)} \longrightarrow H^+_{(aq)} + CH_3CO_2^-_{(aq)}$ $K_{a} = \frac{[H^{+}_{(aq)}][CH_{3}CO_{2}_{(aq)}]}{[CH_{3}CO_{2}_{(aq)}]} \longrightarrow K_{a} = \frac{[H^{+}_{(aq)}]^{2}}{[CH_{3}CO_{2}H_{(aq)}]_{initial}} \longrightarrow 1.7 \times 10^{-5} = \frac{[H^{+}_{(aq)}]^{2}}{0.01}$ $[CH_3CO_2H_{(aq)}]$ $[H_{(a0)}^+]_2 = 1.7 \times 10^{-5} \times 0.01$ $pH = -\log [H^+] = -\log (4.12 \times 10^{-4})$ pH =3.38 $[H_{(aq)}^{+}] = 1.7 \times 10^{-7} = 4.12 \times 10^{-4}$

Example 6 Calculate the concentration of propanoic acid with a pH of 3.52 (ka is
$$1.35 \times 10^{-5} \text{ mol dm}^{-3}$$
)

$$CH_{3}CH_{2}CO_{2}H_{(aq)} \longrightarrow H^{+}_{(aq)} + CH_{3}CH_{2}CO_{2}^{-}_{(aq)}$$

$$[H^{+}] = 1 \times 10^{-3.52} = 0.000302M$$

$$Ka = \frac{[H^{+}_{(aq)}][CH_{3}CH_{2}CO_{2}^{-}_{(aq)}]}{[CH_{3}CH_{2}CO_{2}H_{(aq)}]} \longrightarrow Ka = \frac{[H^{+}_{(aq)}]^{2}}{[CH_{3}CH_{2}CO_{2}H_{(aq)}]} \longrightarrow 1.35 \times 10^{-5} = \frac{[0.000302]^{2}}{[CH_{3}CH_{2}CO_{2}H_{(aq)}]}$$

$$[CH_{3}CH_{2}CO_{2}H_{(aq)}] = 9.12 \times 10^{-8} / 1.35 \times 10^{-5} \qquad [CH_{3}CH_{2}CO_{2}H_{(aq)}] = 6.75 \times 10^{-3} \text{ mol dm}^{-3}$$

pH Calculations involving Neutralisation Reactions

These can be quite complex calculations working out the pH of a partially neutralised acid or the pH of the solution if too much alkali has been added and has gone past neutralisation. The method differs if the acid is strong or weak for the partially neutralised case.



Strong diprotic acids and bases

Questions of the type in Example 7 and 8 may include strong diprotic acids such as H_2SO_4 or bases such as $Ba(OH)_2$.

Example 9 35cm³ of 0.5 mol dm⁻³ H₂SO₄ is reacted with 30cm³ of 0.55 mol dm⁻³ NaOH. Calculate the pH of the resulting mixture. Moles H₂SO₄ = conc x vol = 0.5 x 0.035 = 0.0175mol Moles H⁺ = 0.0175 x2 = 0.035 Moles NaOH =mol OH⁻ = conc x vol = 0.55 x 0.030 = 0.0165 H⁺ + OH⁻ \rightarrow H₂O Moles of H⁺ in excess = 0.035 -0.0165 = 0.0185 [H⁺] = moles excess H⁺ total volume (dm³) = 0.0185/ 0.065 = 0.28 mol dm⁻³ pH = - log [H⁺] = -log 0.28 = 0.55 **Example 10** 15cm³ of 0.5mol dm⁻³ HCl is reacted with 35cm³ of 0.45 mol dm⁻³ **Ba(OH)**₂. Calculate the pH of the resulting mixture.

Moles $HCI = mol H^+ = conc x vol = 0.5 x 0.015 = 0.0075 mol$

Moles $Ba(OH)_2 = conc x vol = 0.45 x 0.035 = 0.01575$

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Moles OH<sup>-</sup> = 0.01575 x2 = 0.0315
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H<sup>+</sup> + OH<sup>-</sup> → H<sub>2</sub>O

Moles of OH<sup>-</sup> in excess = 0.0315 - 0.0075= 0.024

[OH<sup>-</sup>] = <u>moles excess OH<sup>-</sup></u>

total volume (dm<sup>3</sup>)

= 0.024/ 0.05 = 0.48 mol dm<sup>-3</sup>

[H<sup>+</sup>] = K<sub>w</sub>/[OH<sup>-</sup>]

= 1x10<sup>-14</sup> / 0.48 = 2.08x10<sup>-14</sup>

pH = -log [H<sup>+</sup>]

= -log 2.08x10<sup>-14</sup>

= 13.68
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Weak Acid and Strong Base Neutralisations



total volume (dm³) total volume (dm³) = 0.01875/ 0.08 = 0.234M = 0.00875/ 0.08 = 0.109M $ka = [H^+] [CH_3CO_2^-]$ $[H^+] = ka x [CH_3CO_2H] / [CH_3CO_2^-]$ $[CH_3CO_3H]$ $pH = -\log [H^+]$ = 1.7 x 10⁻⁵ x 0.234 / 0.109 $= -\log 3.64 \times 10^{-5}$ = 4.44 = 3.64 x 10⁻⁵

Working out pH of a weak acid at half equivalence

When a weak acid has been reacted with exactly half the neutralisation volume of alkali, the above calculation can be simplified considerably. At half neutralisation we can make the

ka = [<u>H+] [CH₃CO₂]</u> $[CH_3CO_2H]$ assumption that [HA] = [A-]

So $[H^+_{(aq)}] = ka$

And pH = pka

Example 12

Calculate the pH of the resulting solution when 25cm³ of 0.1M NaOH is added to 50cm³ of 0.1M CH₃COOH (ka 1.7 x 10⁻⁵)

From the volumes and concentrations spot it is half neutralisation (or calculate)

 $pH = pka = -log(1.7 \times 10^{-5}) = 4.77$



Example 13 Calculate the new pH when 50.0 cm³ of 0.150 mol dm⁻³ HCl is mixed with 500 cm³ of water.

 $[H^{+}_{(aq)}] = 0.150 \text{ x } 0.05 = 0.55$ $[H^+] = [H^+]_{old} \times \underline{old \ volume}$ $[H^{+}_{(aq)}] = 0.0136$ new volume $pH = -\log [H^+]$ = -log 0.0136 = 1.87

Buffer Solutions

A Buffer solution is one where the pH does **not change significantly** if **small** amounts of acid or alkali are added to it.

An **acidic** buffer solution is made from a **weak acid** and a **salt of that weak acid** (made from reacting the weak acid with a strong base).

Example : ethanoic acid and sodium ethanoate

CH₃CO₂H (aq) and CH₃CO₂-Na+

How Buffer solutions work

In an ethanoic acid buffer $CH_3CO_2H_{(aq)} \longrightarrow CH_3CO_2^{-}_{(aq)} + H^+_{(aq)}$ Acid conjugate base

The buffer contains a reservoir of HA and A - ions

If **small amounts of acid is added** to the buffer: Then the above equilibrium will shift to the left removing nearly all the H⁺ ions added,

 $CH_3CO_2^{-}_{(aq)} + H^+_{(aq)} \rightarrow CH_3CO_2H_{(aq)}$

As there is a large concentration of the salt ion in the buffer the ratio $[CH_3CO_2H]/[CH_3CO_2^-]$ stays almost constant, so the pH stays fairly constant.

If **small amounts of alkali is added** to the buffer. The OH⁻ ions will react with H⁺ ions to form water.

 $H^+ + OH^- \rightarrow H_2O$

The Equilibrium will then shift to the right to produce more H⁺ ions.

 $CH_3CO_2H_{(aq)}$ \leftarrow $CH_3CO_2^{-}_{(aq)}$ + $H^+_{(aq)}$

Some ethanoic acid molecules are changed to ethanoate ions but as there is a large concentration of the salt ion in the buffer the ratio $[CH_3CO_2H]/[CH_3CO_2^-]$ stays almost constant, so the pH stays fairly constant.

A **basic** buffer solution is made from a weak base and a salt of that weak base (made from reacting the weak base with a strong acid).

Example :ammonia and ammonium chloride $\rm NH_3~$ and $\rm NH_4^+Cl^-$

In a buffer solution there is a much higher concentration of the salt CH_3CO_2 ion than in the pure acid.

$$[H_{(aq)}^{+}] = Ka \frac{[CH_{3}CO_{2}H_{(aq)}]}{[CH_{3}CO_{2}(aq)]}$$

Learn these explanations carefully and be able to write the equilibrium to illustrate your answer.

Calculating the pH of Buffer Solutions

We still use the weak acids dissociation expression



If a buffer is made by adding sodium hydroxide to partially neutralise a weak acid then follow the method below

Example 16 55cm³ of 0.5 mol dm⁻³ CH₃CO₂H is reacted with 25cm³ of 0.35 mol dm⁻³ NaOH. Calculate the pH of the resulting buffer solution. CH₃CO₂H+ NaOH → CH₃CO₂Na + H₂O Moles $CH_3CO_2H = conc x vol = 0.5x 0.055 = 0.0275mol$ ka is 1.7 x 10⁻⁵ mol dm⁻³ Moles NaOH = conc x vol = 0.35 x 0.025 = 0.00875 Moles of CH₃CO₂H in excess = 0.0275-0.00875 = 0.01875 (as 1:1 ratio) $[CH_3CO_2H] = moles excess CH_3CO_2H$ $[CH_3CO_2^-] = moles OH^- added$ total volume (dm³) total volume (dm³) = 0.01875/ 0.08 = 0.234M = 0.00875/ 0.08 = 0.109M $ka = [H^+] [CH_3CO_2^-]$ $[H^+] = ka x [CH_3CO_2H] / [CH_3CO_2^-]$ $[CH_3CO_2H]$ $pH = -\log [H^+]$ = 1.7 x 10⁻⁵ x 0.234 / 0.109 $= -\log 3.64 \times 10^{-5}$ $= 3.64 \times 10^{-5}$ = 4.44

= -log 5.07x 10⁻⁵ = 4.29

If a small amount of alkali is added to a buffer then the moles of the buffer acid would reduce by the number of moles of alkali added and the moles of salt would increase by the same amount so a new calculation of pH can be done with the new values.

 $CH_3CO_2H_{(aq)} + OH^- \rightarrow CH_3CO_2^{-}_{(aq)} + H_2O_{(l)}$

If a small amount of acid is added to a buffer then the moles of the buffer salt would reduce by the number of moles of acid added and the moles of buffer acid would increase by the same amount so a new calculation of pH can be done with the new values.

 $CH_3CO_2^-_{(aq)} + H^+ \rightarrow CH_3CO_2H_{(aq)}$

Example 17: 0.005 mol of NaOH is added to 500cm³ of a buffer where the concentration of ethanoic acid is 0.200 mol dm⁻³ and the concentration of sodium ethanoate is 0.250 mol dm⁻³. (Ka = 1.7×10^{-5})

Calculate the pH of the buffer solution after the NaOH has been added.

Work out the moles of acid and salt in the initial buffer solution Moles ethanoic acid= conc x vol = 0.200 x 0.500 = 0.100mol Moles sodium ethanoate = conc x vol = 0.25 x 0.500 = 0.125mol

Work out the moles of acid and salt in buffer after the addition of 0.005mol NaOH Moles ethanoic acid = 0.100 - 0.005 = 0.095 mol Moles sodium ethanoate = 0.125 +0.005 = 0.130 mol We can enter moles of acid and salt straight

$$[H_{(aq)}^{+}] = Ka \quad \frac{[CH_{3}COOH_{(aq)}]}{[CH_{3}COO_{(aq)}]} \leq$$

they both have the same new final volume $[H_{(aq)}^{+}] = 1.7 \times 10^{-5} \times \frac{0.095}{0.130} \rightarrow [H_{(aq)}^{+}] = 1.24 \times 10^{-5}$ $pH = -\log [H^+]$ = -log 1.24x 10⁻⁵

into the equation as

= 4.91

Titration curves

Constructing a pH curve Calibrate meter first by measuring known pH of a Transfer 25cm³ of acid to a conical flask with a volumetric 1. buffer solution. This is necessary because pH meters pipette can lose accuracy on storage. Measure initial pH of the acid with a pH meter 2. Most pH probes are calibrated by putting probe in a Add alkali in small amounts (2cm³) noting the volume 3. set buffer (often pH 4) and pressing a calibration added button/setting for that pH. Sometimes this is Stir mixture to equalise the pH 4. repeated with a second buffer at a different pH 5. Measure and record the pH to 1 d.p. Repeat steps 3-5 but when approaching endpoint add in 6. smaller volumes of alkali

7. Add until alkali in excess

Can also improve accuracy by maintaining constant temperature



Weak acid – Strong base e.g. CH₃CO₂H and NaOH

At the start the pH rises quickly and then levels off. The flattened part is called the buffer region and is formed because a buffer solution is made





Strong acid – Weak base

e.g. HCl and NH₃



Weak acid – Weak base

e.g. CH₃CO₂H and NH₃



Choosing an Indicator

Indicators can be considered as weak acids. The acid must have a different colour to its conjugate base

An indicator changes colour from HIn to In⁻ over a narrow range. Different indicators change colours over different ranges.

The end-point of a titration is defined as the point when the colour of the indicator changes colour

The end-point of a titration is reached when $[HIn] = [In^{-}]$. To choose a correct indicator for a titration one should pick an indicator whose end-point coincides with the equivalence point for the titration.

How indicators work

HIn (aq) $in_{(aq)} + H_{(aq)}$ colour A colour B

We can apply Le Chatelier to give us the colour.

In an acid solution the H⁺ ions present will push this equilibrium towards the reactants. Therefore colour A is the acidic colour.

In an alkaline solution the OH^- ions will react and remove H^+ ions causing the equilibrium to shift to the products. Colour B is the alkaline colour.

An indicator will work if the pH range of the indicator lies on the **steep** part of the titration curve. In this case the indicator will change colour rapidly and the colour change will correspond to the neutralisation point.

pН Only use phenolphthalein in titrations with strong strong base 13 bases but not weak bases-Colour change: colourless acid \rightarrow pink alkali pH range for weak base phenolphthalein 7 Use methyl orange with titrations with pH range for weak acid strong acids but not weak acids methyl orange Colour change: red acid \rightarrow yellow alkali strong acid (orange end point) cm³ of base 25